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Oxidation Number

The charge the atom would have in a molecule (or an ionic compound) if electrons were completely transferred.

1. Free elements (uncombined state) have an oxidation number of zero

Na, Be, K, Pb, H_2 , O₂, P₄ = 0

2. In monatomic ions, the oxidation number is equal to the charge on the ion.

 Li^+ , $Li = +1$; Fe^{3+} , $Fe = +3$; O^{2-} , $O = -2$

3. The oxidation number of oxygen *is* **usually −2**. In $H_2 O_2$ and O_2^{2-} it is -1.

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Balancing Redox Equations 3

7. Add the two half-reactions together and balance the final equation by inspection**. The number of electrons on both sides must cancel.**

> Oxidation : $6Fe^{2+} \rightarrow 6Fe^{3+} + \cancel{6}e^{-}$ $\text{Reduction}: \cancel{6} \cancel{\epsilon}^{-} + 14\text{H}^{+} + \text{Cr}_2\text{O}_7{}^{2-} \rightarrow 2\text{Cr}^{3+} + 7\text{H}_2\text{O}$

 $14H^+ + Cr_2O_7^{2-} + 6Fe^{2+} \rightarrow 6Fe^{3+} + 2Cr^{3+} + 7H_2O$

8. Verify that the number of atoms and the charges are balanced.

 $14 \times 1 - 2 + 6 \times 2 = 24 = 6 \times 3 + 2 \times 3$

9. For reactions in basic solutions, add OH- to **both sides** of the equation for every H⁺ that appears in the final equation.

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Example 18.1 ²

Strategy

We follow the preceding procedure for balancing redox equations. Note that the reaction takes place in a basic medium.

Solution

Step 1: The unbalanced equation is

$$
MnO_4^- + I^- \rightarrow MnO_2 + I_2
$$

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Example 18.1 4

To balance charges, we add two electrons to the righthand side of the equation:

 $2I^{-} \rightarrow I_{2} + 2e^{-}$

Reduction half-reaction: To balance the O atoms, we add two H2O molecules on the right:

 $MnO₄ \rightarrow MnO₂ + 2H₂O$

To balance the H atoms, we add four H^+ ions on the left:

 $MnO_4^- + 4H^+ \rightarrow MnO_2 + 2H_2O$

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Example 18.1 6

The electrons on both sides cancel, and we are left with the balanced net ionic equation:

 $6I^{-}$ + $2MnO₄⁻$ + $8H^{+}$ \rightarrow $3I₂$ + $2MnO₂$ + $4H₂O$

This is the balanced equation in an acidic medium. However, because the reaction is carried out in a basic medium, for every H⁺ ion we need to add equal number of OH⁻ ions to both sides of the equation:

 $6I^{-}$ + $2MnO_{4}^{-}$ + $8H^{+}$ + $8OH^{-}$ \rightarrow $3I_{2}$ + $2MnO_{2}$ + $4H_{2}O$ + $8OH^{-}$

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Galvanic Cells CuSO₄ solutio $Cu²⁺$ is reduced
to Cu at cathode Zn is oxidized
to Zn^{2+} at anode Net reaction + $Cu^{2+}(aq)$ - \rightarrow Zn²⁺(aq) - $(s) + Cu^{2+}(aq) \longrightarrow Zn^{2+}(aq) + Cu$

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Example 18.2 ²

Strategy

To predict what redox reaction(s) will take place, we need to compare the standard reduction potentials of Cl_2 , Br_2 , and I_2 and apply the diagonal rule.

Solution

From Table 18.1, we write the standard reduction potentials as follows: C_1 (1 etm) $2c^2 \sqrt{2}C^{1-}(1 M)$ $E^0 = 1.36 M$

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Example 18.3¹

A galvanic cell consists of a Mg electrode in a 1.0 *M* Mg(NO3)2 solution and an Ag electrode in a 1.0 *M* AgNO₃ solution. Calculate the standard emf of this cell at 25°C.

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Example 18.3 ²

Strategy

At first it may not be clear how to assign the electrodes in the galvanic cell. From Table 18.1 we write the standard reduction potentials of Ag and Mg and apply the diagonal rule to determine which is the anode and which is the cathode.

Solution

The standard reduction potentials are

 $Ag^+(1.0 M) + e^- \rightarrow Ag(s)$ $E^{\circ} = 0.80 V$

$$
Mg^{2+}(1.0 M) + 2e^- \to Mg(s) \qquad E^{\circ} = -2.31 V
$$

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Example 18.3 ₃

Applying the diagonal rule, we see that Ag⁺ will oxidize Mg:

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Example 18.3 4

Note that in order to balance the overall equation we multiplied the reduction of $Ag⁺$ by 2. We can do so because, as an intensive property, *E*° is not affected by this procedure. We find the emf of the cell by using Equation (18.1) and Table 18.1:

$$
E_{\text{cell}}^{\circ} = E_{\text{ cathode}}^{\circ} - E_{\text{anode}}^{\circ}
$$

= $E_{\text{Ag}^{+}/\text{Ag}}^{\circ} - E_{\text{Mg}^{2+}/\text{Mg}}^{\circ}$
= 0.80 V - (-2.37 V)
= 3.17 V

Check

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The positive value of E° shows that the forward reaction is favored.

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Spontaneity of Redox Reactions $\Delta G = -nFE_{cell}$ $n =$ number of moles of electrons in reaction $\Delta G^{\circ} = -nFE^{\circ}_{cell}$ $F = 96,500 \frac{J}{V \cdot mol} = 96,500 C/mol$ $\Delta G^{\circ} = -RT \ln K = -nFE^{\circ}_{cell}$ $E_{\text{cell}}^{\circ} = \frac{RT}{nF} \ln K = \frac{(8.314 \cancel{J/K} \cdot \cancel{\text{mod}})(298 \cancel{K})}{n(96,500 \cancel{J/V} \cdot \cancel{\text{mod}})} \ln K$ $\frac{S}{\sqrt{2}}$ $E_{\text{cell}}^{\circ} = \frac{0.0257 \text{ V}}{\text{n}} \ln K$ $\Delta G^{\circ}=-{RT}{\rm ln}K$ $E_{\text{cell}}^{\circ} = \frac{0.0592 \text{ V}}{\text{n}} \log K$ Access the text alternative for slide images.

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Example 18.4

Calculate the equilibrium constant for the following reaction at 25°C:

$$
\mathrm{Sn}\left(s\right) + 2\mathrm{Cu}^{2+}\left(aq\right) \leftrightarrow \mathrm{Sn}^{2+}\left(aq\right) + 2\mathrm{Cu}^{+}\left(aq\right)
$$

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© McGraw Hill LLC Example 18.4 2 *Strategy* The relationship between the equilibrium constant *K* and the standard emf is given by Equation (18.5): $E_{\text{cell}}^{\circ} = (0.0257 \text{ V}/n) \ln K$ Thus, if we can determine the standard emf, we can calculate the equilibrium constant. We can determine the E_{cell}° of a hypothetical galvanic cell made up of two couples $\left(\frac{\text{Sn}^{2+}}{\text{Sn}} \right)$ and Cu^{2+}/Cu) from the standard reduction potentials in Table 18.1.

© McGraw Hill LLC Example 18.4 3 *Solution* The half-cell reactions are Anode(oxidation): $\text{Sn}(s) \to \text{Sn}^{2+}(aq) + 2e^{-}$ $\text{Cathode}(\text{reduction}) : 2\text{Cu}^{2+}(aq) + 2e^- \rightarrow 2\text{Cu}^+(aq)$ $E_{\text{cell}}^{\circ}=E_{\text{ cathode}}^{\circ}-E_{\text{ anode}}^{\circ}$ $=E^{^{\circ}}_{\text{Cu}^{2+}/\text{Cu}^{+}} - E^{^{\circ}}_{\text{Sn}^{2+}/\text{Sn}}$ $= 0.15V - (-0.14V)$ $= 0.29V$ 33

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Example 18.5¹

Calculate the standard free-energy change for the following reaction at 25°C:

 $2Au (s) + 3Ca²⁺ (1.0 M) \rightarrow 2Au³⁺ (1.0 M) + 3Ca (s)$

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Example 18.5 ²

Strategy

The relationship between the standard free energy change and the standard emf of the cell is given by Equation (18.3): $\Delta G^{\circ} = -nFE^{\circ}_{cell}$.

Thus, if we can determine E_{cell}° we can calculate ΔG° We can determine the E_{cell}° of a hypothetical galvanic cell made up of two couples (Au^{3+}/Au) and Ca^{2+}/Ca from the standard reduction potentials in Table 18.1.

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                                  Example 18.5 <sub>3</sub>
Solution 
The half-cell reactions are
        Anode (oxidation): 2Au (s) \rightarrow 2Au^{3+}(1.0M) + 6e^{-t}Cathode (Reduction): 3Ca^{2+}(1.0M) + 6e^- \rightarrow 3Ca(s)E_{\text{cell}}^{\circ} = E_{\text{ cathode}}^{\circ} - E_{\text{anode}}^{\circ}=E^{^{\circ}}_{\text{Ca}^{2+}/\text{Ca}}-E^{^{\circ}}_{\text{Au}^{2+}/\text{Au}}=- 2.87 V - 1.50 V=-4.37V
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The Effect of Concentration on Cell Emf $\Delta G = \Delta G^{\circ} + RT \ln Q$ $\Delta G = -nFE$ $\Delta G^{\circ} = -nFE^{\circ}$ $-nFE = -nFE^{\circ} + RT \ln Q$ **Nernst** equation $E = E^{\circ} - \frac{RT}{nF} \ln Q$ At 298 K $E = E^{\circ} - \frac{0.0257 \text{ V}}{n} \ln Q$ $E = E^{\circ} - \frac{0.0592 \text{ V}}{n} \log Q$ 39

Example 18.6 Predict whether the following reaction would proceed spontaneously as written at 298 K: $\text{Co}(s)$ + Fe²⁺ (aq) \rightarrow Co²⁺ (aq) + Fe(s) given that $\left[\text{Co}^{2+}\right] = 0.15 M$ and $\left[\text{Fe}^{2+}\right] = 0.68 M$. C McGraw Hill Ll

Example 18.6 ²

Strategy

Because the reaction is not run under standard-state conditions (concentrations are not 1 *M*), we need Nernst's equation [Equation (18.8)] to calculate the emf (E) of a hypothetical galvanic cell and determine the spontaneity of the reaction. The standard emf (E°) can be calculated using the standard reduction potentials in Table 18.1. Remember that solids do not appear in the reaction quotient (*Q*) term in the Nernst equation. Note that 2 moles of electrons are transferred per mole of reaction, that is, $n = 2$.

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Example 18.7²

Strategy

The equation that relates standard emf and nonstandard emf is the Nernst equation. The overall cell reaction is

 $Zn(s) + 2H^+(?M) \rightarrow Zn^{2+}(1.0M) + H_2(1.0atm)$

Given the emf of the cell (E) , we apply the Nernst equation to solve for $[H^+]$. Note that 2 moles of electrons are transferred per mole of reaction; that is, $n = 2$.

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Example 18.7⁴

Check

The fact that the nonstandard-state emf (E) is given in the problem means that not all the reacting species are in their standard-state concentrations. Thus, because both Zn^{2+} ions and H_2 gas are in their standard states, $[H^+]$ is not 1 M.

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An aqueous Na2SO4 solution is electrolyzed, using the apparatus shown in Figure 18.18. If the products formed at the anode and cathode are oxygen gas and hydrogen gas, respectively, describe the electrolysis in terms of the reactions at the electrodes.

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Example 18.8 2

Strategy

Before we look at the electrode reactions, we should consider the following facts: (1) Because NaSO₄ does not hydrolyze, the pH of the solution is close to 7. (2) The Na^+ ions are not reduced at the cathode and the SO_4^{2-} ions are not oxidized at the anode. These conclusions are drawn from the electrolysis of water in the presence of sulfuric acid and in aqueous sodium chloride solution, as discussed earlier. Therefore, both the oxidation and reduction reactions involve only water molecules.

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Example 18.8 ₃

Solution

The electrode reactions are

Anode: $2H_2O(l) \to O_2(g) + 4H^+(aq) + 4e^{-}$ Cathode: $2H_2O(l) + 2e^- \rightarrow H_2(g) + 2OH^-(aq)$ Anode: Cathode:

The overall reaction, obtained by doubling the cathode reaction coefficients and adding the result to the anode reaction, is

$$
6H_2O(l) \rightarrow 2H_2(g) + O_2(g) + 4H^+(aq) + 4OH^-(aq)
$$

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Example 18.9

A current of 1.26 A is passed through an electrolytic cell containing a dilute sulfuric acid solution for 7.44 h. Write the half-cell reactions and calculate the volume of gases generated at STP.

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Example 18.9 3

According to Figure 18.20, we carry out the following conversion steps to calculate the quantity of O_2 in moles:

current × time \rightarrow coulombs \rightarrow moles of $e^- \rightarrow$ moles of O₂

Then, using the ideal gas equation we can calculate the volume of O_2 in liters at STP. A similar procedure can be used for H2.

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Example 18.9 4

Solution

First we calculate the number of coulombs of electricity that pass through the cell:

?C = 1.26
$$
\cancel{K} \times 7.44 \cancel{K} \times \frac{3600 \cancel{K}}{1 \cancel{K}} \times \frac{1 \text{C}}{1 \cancel{K} \cdot \cancel{K}} = 3.37 \times 10^4 \text{C}
$$

Next, we convert number of coulombs to number of moles of electrons

$$
3.37 \times 10^4 \text{ g}^{\prime} \times \frac{1 \text{ mol } e^-}{96,500 \text{ g}^{\prime}} = 0.349 \text{ mol } e^-
$$

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Example 18.9 s

From the oxidation half-reaction we see that 1 mol $O_2 = 4$ mol e^- . Therefore, the number of moles of O_2 generated is

0.349
$$
\mu\text{o}f
$$
 $e^{-} \times \frac{1 \text{ mol } O_2}{4 \text{ mol } e^{-}} = 0.0873 \text{ mol } O_2$

The volume of 0.0873 mol O_2 at STP is given by

$$
V = \frac{nRT}{P}
$$

= $\frac{(0.0873 \text{ mol})(0.0821 \text{ L} \cdot \text{atm/K} \cdot \text{mol})(273 \text{ K})}{1 \text{atm}}$ = 1.96 L

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Example 18.9,

Check

Note that the volume of H_2 is twice that of O_2 (see Figure 18.18), which is what we would expect based on Avogadro's law (at the same temperature and pressure, volume is directly proportional to the number of moles of gases).

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