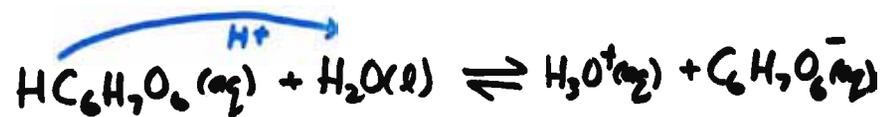


How can we measure K_a from pH?

ex: pH of a 0.20M soln of $\text{HC}_6\text{H}_7\text{O}_6(\text{aq})$ @ 25°C, $\text{pH} = 2.40$
What's its K_a ?



| | | | | |
|---|----------|---|-----|-----|
| I | 0.20M | — | ≈ 0 | 0 |
| C | -x | — | +x | +x |
| E | (0.20-x) | — | (x) | (x) |

$$K_a = \frac{[\text{H}_3\text{O}^+][\text{C}_6\text{H}_7\text{O}_6^-]}{[\text{HC}_6\text{H}_7\text{O}_6]_{\text{eq}}}$$

?

$$K_a = \frac{(x)(x)}{0.20-x}$$

$$\Rightarrow K_a = \frac{(4.0 \times 10^{-3})^2}{0.20 - 4.0 \times 10^{-3}} = 8.1 \times 10^{-5}$$

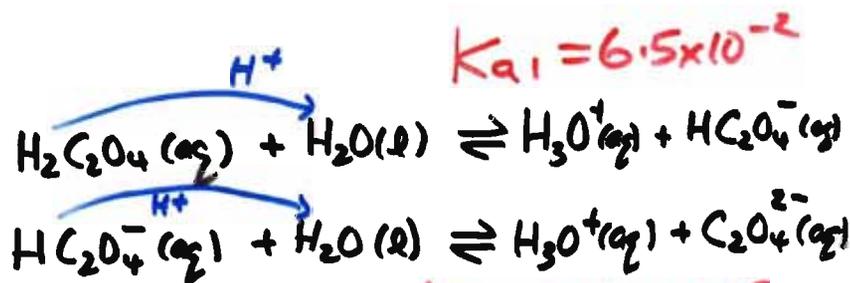
$$\begin{aligned} \text{pH} &= -\log_{10} [\text{H}^+] \\ [\text{H}^+] &= 10^{-\text{pH}} \\ \text{2sf. } x &= 10^{-2.40} \\ &= 4.0 \times 10^{-3} \end{aligned}$$

Monoprotic acid 1 H^+ /molecule: HCl
Diprotic acid 2 H^+ /molecule:



Polyprotic acid > 1 H^+ /molecule

ex: oxalic acid: $\text{H}_2\text{C}_2\text{O}_4$



$$K_{a1} = 6.5 \times 10^{-2}$$

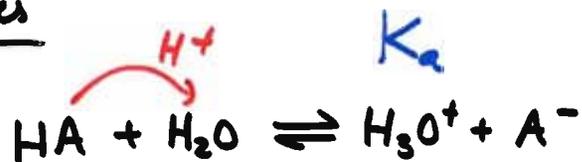
$$K_{a2} = 6.1 \times 10^{-5}$$

in general: $K_{a1} > K_{a2} > K_{a3} > \dots$

→ successively smaller

Weak Bases

acids,
HA



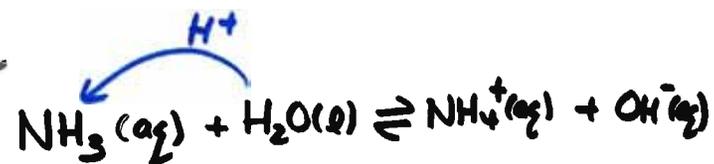
weak base,
B



$$K_b = \frac{[\text{BH}^+][\text{OH}^-]}{[\text{B}]_{\text{eq}}}$$

ex: Ammonia is a weak base,
 $K_b = 1.8 \times 10^{-5}$ @ 25°C.
What's pH of a 0.50 M soln?

ICE-Chart



| | | | | |
|---|---------|---|-----|-----|
| I | 0.50M | — | 0 | ≈ 0 |
| C | -x | — | +x | +x |
| E | (0.5-x) | — | (x) | (x) |

$$K_b = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]_{\text{eq}}}$$

PH?

$$1.8 \times 10^{-5} = \frac{(x)(x)}{0.5-x}$$

Assume: $x \ll 0.5$

$$1.8 \times 10^{-5} \approx \frac{(x)(x)}{0.50}$$
$$\Rightarrow \sqrt{(1.8 \times 10^{-5})(0.5)} = \sqrt{x^2} = x$$

$$\Rightarrow x = 3.0 \times 10^{-3}$$

Check Assumption: 5% rule.

< 5% dissociated (✓)

$$\% \text{ dissoci.} = \frac{[\text{OH}^-]_{\text{eq}} \times 100}{[\text{B}]_0}$$

$$= \frac{3 \times 10^{-3} \text{ M}}{0.50 \text{ M}} \times 100$$

$$= 0.6\% \quad (\checkmark)$$

$$\Rightarrow [\text{OH}^-] = 3.0 \times 10^{-3} \text{ M} \quad \text{2sf.}$$

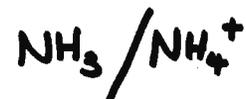
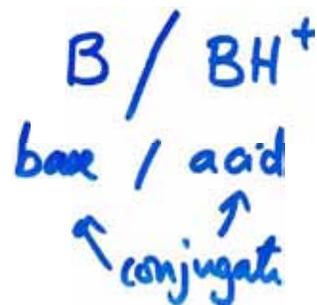
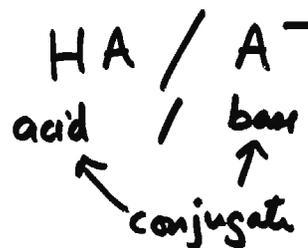
$$\text{pOH} = -\log_{10} [\text{OH}^-]$$

$$= 2.52$$

$$\Rightarrow \text{pH} = 14.00 - \text{pOH} = 11.48$$

$$\Rightarrow \text{pH} + \text{pOH} = 14.00 \quad (25^\circ\text{C}) \quad \text{BASIC}$$

Conjugate ACID-BASE pairs



K_a and K_b for conj. pairs are related!

$$\boxed{K_a \cdot K_b = K_w}$$

at any temp

ex. HCN
hydrocyanic
acid

$$K_a = 4.9 \times 10^{-10}$$

@ 25°C

$$K_a \cdot K_b = K_w$$

CN⁻
cyanide

$$K_b = \frac{K_w}{K_a}$$
$$= \frac{1.0 \times 10^{-14}}{4.9 \times 10^{-10}}$$
$$= 2.0 \times 10^{-5}$$